

Answer **ANY 4** of the following:

(4×5=20)

**Q1.]** If  $X = \{1, 2, 3, \dots, 15\}$  is the universal set,  $A = \{1, 3, 5, 8, 9, 10, 12, 15\}$   
 $B = \{2, 3, 4, 6, 8, 9, 10, 11, 13\}$   $C = \{1, 2, 5, 8, 9, 14\}$  Verify De-Morgan's law & Distributive laws.

**Q2.]** If  $X$  is the universal set and  $A$  &  $B$  are subset of  $X$  such that  $n(X) = 99$ ,  $n(A^c) = 80$ ,  
 $n(B^c) = 85$  and  $n[(A \cap B)^c] = 94$ . Find  $n(A \cup B)$ .

**Q3.]** If  $f(x) = x^2 + 3x - 5$ ,  $0 \leq x \leq 6$  find  $f(0)$ ,  $f(2)$ ,  $f(4)$ ,  $f(7)$ , whenever they exist also  
find  $x$  if  $f(x) = 35$ .

**Q4.]** Find  $f\{g(x)\}$  &  $g\{f(x)\}$  if

a)  $f(x) = x^2$                        $g(x) = 5x - 6$

b)  $f(x) = x^2 + 4$                        $g(x) = \frac{1}{x}$

**Q5.]** Define an Equivalence Relation. Let  $A = \{x \mid x < 4, x \in \mathbb{N}\}$ . A relation  $R$  on the set  $A$  is  
given by  $R = \{(1, 1), (1, 2), (2, 1), (2, 3), (3, 2)\}$  prove that  $R$  is symmetric relation but it is  
neither reflexive nor transitive.

**Q6.]** Prove that the relation  $R$  on the set of integer  $\mathbb{Z}$  defined as

$$R = \{(x, y) \mid x - y \text{ is divisible by } 3, x \in \mathbb{Z}, y \in \mathbb{Z}\} \text{ is an equivalence relation.}$$

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