Goa Vidyaprasarak Mandal's
Gopal Govind Poy Raiturcar College of Commerce and Economics Farmagudi Ponda Goa
B.Com. (Semester II) Examination, April 2017

MATHEMATICAL TECHNIQUES

## Duration:- 2 Hours

Q1 Attempt the following.
$(4 \times 5=20)$
a) In how much time will Rs. 5,000 at $3 \%$ p.a. produce the same income as Rs. 10,000 in 2 years at $3 \%$ p.a. simple interest?
b) Show that the points $(5,4),(2,3)$, and $(1,0)$ are the vertices of an isosceles triangle.
c) A function $f$ is given as:

$$
f(x)= \begin{cases}3 x+5, & \text { for }-3 \leq x<-1 \\ 2 x+1, & \text { for }-1 \leq x<2 \\ 2-x, & \text { for } 2 \leq x \leq 4\end{cases}
$$

Find $f(-2), f(2), f(3), f(1)$.
d) Find $\frac{d y}{d x}$
i) $y=x^{2} \log x$
ii) $y=\left(a^{x}-5 x+4\right)^{5}$
e) Find the equation of line having slope $3 / 4$ and Y-intercept -6.

## OR

## QI Attempt the following.

p) In how many years will sum of money be doubled at $25 \%$ p.a. simple interest?
q) $\mathrm{A}(2,1)$ and $\mathrm{B}(4,3)$ are two points. If B is the mid-point of segment AC , find the co-ordinates of the point C .
r) If $f(x)=2 x^{2}-3 x+1$, for what value of x is $f(2 x)=2 f(x)$ ?
s) Differentiate with respect to x
i) $y=\frac{3 x+5}{5 x-7}$
ii) $y=\sqrt{3 x^{2}+2+e^{x}}$
t) Find the equation of the line passing through the point of intersection of the lines $2 x+y=3, x-3 y=12$ and through the point $(2,3)$.
a) Find the value of x if the triangle whose vertices are $\mathrm{A}(\mathrm{x},-4), \mathrm{B}(2,3)$ and $\mathrm{C}(4,-1)$ is right angled at C .
b) What sum of money will amount to Rs.73,502.58 in 3 years at $7 \%$ p. a. compound interest?
c) Find i) $\lim _{x \rightarrow 2} \frac{x^{2}-7 x+10}{x^{2}-4} \quad$ ii) $\lim _{x \rightarrow 0} \frac{\sqrt{4+x}-\sqrt{4-x}}{x}$
d) Evaluate the following integrals:
i) $\int(x-3)(x+5) d x$
ii) $\int\left(3 x+\frac{2}{x}-e^{x}\right) d x$
e) The demand function for a commodity is given by $\mathrm{p}=16-\frac{x^{2}}{4}$. Find i) the total revenue function and ii) marginal revenue at $\mathrm{x}=1$.

OR
QII Attempt the following.
$(4 \times 5=20)$
p) $A(m, 5)$ and $B(-4, n)$ are the end point of a segment and $C(2,-1)$ is the midpoint. Find $m$ and $n$.
q) Find the future value of Rs. $20,00,000$ after 3 years if the compound interest rate is $8 \%$ p.a.
r) Examine for continuity at $x=0$, the function

$$
f(x)= \begin{cases}\frac{\sqrt{2+x}-\sqrt{2-x}}{x} & \text { for } x \neq 0 \\ 0 & \text { for } x=0\end{cases}
$$

s) Evaluate the following integrals:
i) $\int \frac{x^{4}-6}{x^{2}} d x$
ii) $\int(3 x+4)(2 x-3) d x$
t) At what rate of compound interest would an amount double itself in 3 years? Given that $2^{\frac{1}{3}}=1.2611$ approximately.

## Q3 Attempt the following.

a) Solve the following L.P.P. by graphical method.

Maximize $Z=800 x+100 y$ subject to

$$
\begin{aligned}
& 4 x+6 y \leq 120 \\
& 10 x+3 y \leq 180 \\
& x \geq 0, \quad y \geq 0 .
\end{aligned}
$$

b) Find the maximum and minimum value of the function

$$
f(x)=x^{3}-2 x^{2}+x+10
$$

c) If $D=25-3 p-p^{2}$ is a demand function, find elasticity of demand when $p=3$.
d) If $u=x^{3}+x^{2} y+y^{3}$, prove that

$$
x \frac{\delta u}{\delta x}+y \frac{\delta u}{\delta y}=3 u .
$$

e) Differentiate with respect to x
i) $y=\left(x^{3}+4\right)(1+\log x)$
ii) $y=\frac{x^{2}-1}{2 x+1}$

## OR

## QIII Attempt the following.

p) Solve the following L.P.P. by graphical method.

Minimize $Z=25 x+40 y$ subject to

$$
\begin{aligned}
& x+y \geq 10 \\
& 6 x+4 y \geq 48 \\
& x \geq 0, \quad y \geq 0 .
\end{aligned}
$$

q) The supply function for a commodity is given by $y=20-3 x-3 x^{2}$ where y is demand and x is price. Find the price elasticity of supply when $\mathrm{x}=2$.
r) If $z=3 x^{2}+2 x y+5 x y^{2}$ find $\frac{\delta^{2} z}{\delta x \delta y}$ and $\frac{\delta^{2} z}{\delta y \delta x}$
s) A sum of money amounts to Rs. 45,980 in 3 years and to Rs. 48,640 in 4 years at a certain rate of simple interest. Find the sum and rate.
t) The demand function for a commodity is given by $p=45-3 x-4 x^{2}$. Find the consumers surplus when $\mathrm{x}=2$.

Q 4 Attempt the following.
$(4 \times 5=20)$
a) Find the equation of the line passing through the points $(1,-2)$ and $(-3,4)$.
b) A sum of money is invested for 2 years at a certain rate. If it had been invested at a rate $2 \%$ higher than the present rate, it would have given Rs. 1,300 more as simple interest. Find the sum.
c) Evaluate the integral $\int_{1}^{3}(1-2 x) d x$.
d) Find the total revenue function and demand function, if the marginal revenue function is given as $M R=7-4 x$.
e) The demand function for a commodity is $p=20-2 D-D^{2}$. Find the consumers surplus when $D_{1}=3$.

## OR

Q IV Attempt the following.
$(4 \times 5=20)$
p) Find the equation of the line passing through ( $5,-1$ ) and the sum of whose intercepts on the co-ordinate axes as 8 .
q) A sum of Rs.6,55,000 is invested in a fixed deposit giving $10 \%$ p.a. compound interest. Find the interest in the $4^{\text {th }}$ year.
r) Find the value of $\int_{2}^{3} x(x+1) d x$.
s) The supply function for a commodity is $p=q^{2}+10$. Find the producers surplus when the price per unit of the commodity is Rs. 35 .
t) The marginal cost function for producing x items is given by $M C=$ $3 x^{2}+5 x-4$. Find the total cost function and the average cost function if the fixed cost is Rs. 1000 .

