

#### Goa Vidyaprasarak Mandal's GOPAL GOVIND POY RAITURKAR COLLEGE OF COMMERCE AND **ECONOMICS**

Farmagudi Ponda Goa B.COM. CBCS (Semester II) Examination, April 2018 COMMERCIAL ARITHMETIC

Duration: 2 Hours

## Q1 Attempt the following.

- a) Find k, if the distance between (1, 3) and (2,k) is 5 units.
- b) If  $f(x) = x^2 + 1$ , find x if f(x+1) = f(x+2).
- c) Find  $\frac{dy}{dx}$  for the following: i)  $y = \frac{2x+5}{x-3}$ ii) y = (x+3)(x-1)

- d) If A=(2,2), B=(2,4) and C=(2,6) are the vertices of a triangle ABC, Prove that ABC is an isoceles triangle.
- e) If the total cost in lakhs of rupees for the monthly production of an item is  $C = 50 + 15x - x^2$ , find i) the marginal cost ii) marginal cost when 6 units are produced.

### QI Attempt the following.

 $(4 \times 5 = 20)$ 

- p) Find the point on the x axis whose distance from (7,5) is 13 units.
- q) If  $f(x) = ax^2 + bx + 2$  and f(1) = 3, f(4) = 42, find a and b.

r) Differentiate with respect to x i)  $y = \frac{5x-1}{x+2}$  ii)  $y = (2x^2 + x^2)$ ii) $y = (2x^2 + x + 2^x)$ 

- s) A=(0,3), B=(-2,k) and C=(-1,4) are the vertices of a right angled triangle, right angled at A. Find k.
- t) The demand function is given by  $p = 30 + 6D D^2$ . Find the revenue and marginal revenue when demand is 5 units.

#### Q2 Attempt the following.

 $(4 \times 5 = 20)$ 

- a) A straight line passes through P = (2, -5) and Q = (4,3), find
  - i) Equation of line PQ
  - ii) The value of a if PQ passes through the point (a-1, a+4).
- b) Find  $\lim_{x\to 2} \frac{x^2 4}{x^2 x 2}$
- c) The cost of manufacturing x units is given by  $C = x^2 + 6x + 8$ . Find the average cost and marginal cost at x = 8.
- d) Prove that (-1,2), (3, -1) and (2,6) are the vertices of a right angled triangle.
- e) If  $D = 25 3p p^2$  is a demand function, find the elasticity of demand when p = 3.

OR

#### QII Attempt the following.

 $(4 \times 5 = 20)$ 

- p) Find the equation of line passing through (0,2) and the point of intersection of the lines 4x + 3y 1 = 0 and 3x y + 9 = 0.
- q) Evaluate  $\lim_{x\to 4} \frac{\sqrt{2x+1}-3}{x^2-x-12}$
- r) Differentiate w.r.t. x i)  $y = e^x + 2^x + x^3$  ii)  $y = \frac{3x^2+1}{x-2}$
- s) Write the equation of line parallel to the line 4x 3y + 10 = 0 and passing through (1,4).
- t) If the demand function is given by  $p = 100 3D D^2$ , find the elasticity of demand when D= 5.

# Q3 Attempt the following.

 $(4 \times 5 = 20)$ 

- a) Evaluate the integral  $\int_1^2 (3x^2 + 2x) dx$ .
- b) Solve the following LPP by graphical method. Max Z = 23x + 35y such that

$$4x + 3y \le 40$$

$$2x + 5y \le 55$$

$$x, y \ge 0$$
.



c) Integrate the following w.r.t. x
i) 
$$y = x^6 - 5x^4 + \frac{3}{x} + e^x$$
 ii)  $y = \frac{x^2 - x - 12}{x - 4}$ 

- d) The income of A and B is in the ratio 4:3 and their expenditure is in the ratio 3:2. If each of them save Rs. 600 at the end of a year, find the annual income of each.
- e) The demand function for a commodity is  $p = 20 2x x^2$ . Find the consumers surplus when p = 50.

OR

### QIII Attempt the following.

 $(4 \times 5 = 20)$ 

- p) Given  $f(x) = 100 + 10x 2x^2$ . For what value of x, f(x) is minimum?
- q) q. A company manufactures two types of bags S:small and B: big. The raw materials and labour available per day are 60 units and 50 hours respectively. S requires 2 units of raw material and 5 hours of labour whereas B requires 6 units of raw material and 2 hours of labour. It is observed that, however they try, the total number of bags produced per day, does not exceed 12. Formulate the above problem to maximise the
- r) Integrate the following w.r.t. x

i) 
$$(x+2)(x-3)$$

$$ii)\frac{(x+1)(x+5)}{x}$$

- s) The income of A and B is in the ratio of 4:3 and their expenditure is in the ratio 3:2. If each of them save Rs. 600 at the end of a year, find the annual income of each.
- t) The supply function  $p = 3x^2 + 5$ , find the producers surplus at x = 5.

# Q 4 Attempt the following.

 $(4 \times 5 = 20)$ 

- a) If  $z = 3\frac{x^5}{y^4}$ ; show that  $x\frac{\delta z}{\delta x} + y\frac{\delta z}{\delta y} = z$ .
- b) A person bought a book for Rs. 360. For what price should he sell it to gain 20% ?
- c) The supply function for a commodity is  $p = x^2 + 5x + 4$ , where x is the quantity supplied. Find the producers surplus, when the price is Rs. 10.

- d) The ages of Ram and Shyam are in ratio 5:7 and the difference between their ages is 12 years. Find the present ages of Ram and Shyam.
- e) Bombay Dyeing allows a discount of Rupees 20% on the clothes purchased. Reema purchases clothes worth Rs. 5600. How much will she pay?

OR

Q IV Attempt the following.

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 $(4 \times 5 = 20)$ 

p) If  $z = 2x^3 - 11x^2y + 3y^3$ , show that  $x\frac{\delta z}{\delta x} + y\frac{\delta z}{\delta y} = 3z$ .

- q) If 32 is added to 80% of a number, the result is the number itself. Find the number.
- r) Find the producers surplus at x=3, if the supply function is p = 6x 7.
- s) Nilesh and Ashok are two partners in a firm sharing the profit in the ratio 4:5. If the firm earns profit of Rs. 14130 in 2010, calculate the amount of profit to be received by each partner.
- t) A house owner increase the rent of the house by 15%. Later he decrease it by 10%. Find the percentage change in the house rent.

End