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## Goa Vidyaprasarak Mandal's <br> GOPAL GOVIND POY RAITURCAR COLLEGE OF COMMERCE AND ECONOMICS, PONDA- GOA <br> B.COM. CBCS (SEMESTER - I) EXAMINATION, OCTOBER 2019 COMMERCIAL ARITHMETIC

## Duration: 2 hours

Marks: 80
Instructions: 1. Attempt all questions
2. Figures to the right indicate full marks.

## Q. 1 Attempt the following:

( $5 \times 4=20$ )
a) Construct truth table for $\sim(\sim p \wedge \sim q)$.
b) A certain sum on simple interest becomes `2400 in 2 years and` 2600 in 3 years. Find the principal and rate of simple interest per annum.
c) A college office has 7 men and 5 women, if the committee of 4 members out of these are to selected, find the total number of ways selecting the committee if
i) 3 men and a woman is to be selected
ii) There is no restriction on gender.
d) Find the sum of all numbers from 100 to 300 which are exactly divisible by 5 .
e) If $A=\left[\begin{array}{cc}3 & 1 \\ 1 & -2\end{array}\right]$ and $B=\left[\begin{array}{ll}1 & 5 \\ 3 & 2\end{array}\right]$, find the matrix $X$ such that $3 A+5 B-X=0$. OR

## Q.I Attempt the following:

p) Construct the truth table for $(p \wedge q) \wedge \sim(p \vee q)$.
q) Find compound interest on ` 2400 at $8 \%$ annually for 2 years if
i) the interest is calculated half yearly
ii) the interest is calculated monthly.
r) A 3 digit number is to be formed using the digits from 0 to 9 .

How many such numbers can be formed if the repetition of digits in the number is allowed.
s) If for an A.P. $\mathrm{t}_{26}=103$, find $\mathrm{S}_{51}$.
t) If $M=\left[\begin{array}{cc}1 & -2 \\ 2 & 0\end{array}\right]$ and $N=\left[\begin{array}{ll}2 & 0 \\ 3 & 1\end{array}\right]$, find the matrix $3 M-2 N+I$, where $I$ is the identity matrix of order 2 .

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## Q. 2 Attempt the following:

a) Ajit received 8240 as maturity amount at the end of 2 years on his annuity, the period of payment being end of each year. Find his yearly installment if the rate of interest was $6 \%$ compounded on yearly basis.
b) Using Cramer's rule solve the following equations

$$
3 x+5 y=4 \text { and } x-4 y=2
$$

c) Let $X=\{x / x$ is positive integer less than 10$\}$ be the universal set.

$$
A=\{2,4,7,9\} \text { and } B=\{1,3,5,7\} . \text { Verify }(A \cap B)^{c}=A^{c} \cup B^{c} .
$$

d) Find 3 numbers in G.P. whose sum is 26 and the product is 216 .
e) If ${ }^{n} P_{5}={ }^{n} P_{6}$, find the value of $n$.

## OR

## Q.II Attempt the following:

p) A person is promised the final amount of a half yearly ordinary annuity with periodic payment of ' 1600 , the duration of the annuity being 4 years and the rate of interest is $10 \%$ to be compounded half-yearly. Find the present value of the annuity.
q) Solve the following equations using Cramer's rule,. $2 x+3 y=5, \quad 3 x-5 y=4$
r) The universal set $X=\{1,2,3,4,5,6,7,8\}$. $A=\{2,5,7\}$ and $B=\{3,5,7,8\}$. show that

$$
A \cup B=A \cup(B-A)
$$

s) The third term of a G.P. is 12 and the sixth term is 96 , find its first term and the common ratio.
t) A committee of 5 members is to be formed out of 6 men and 4 women. In how many ways committee can be formed to have at least 3 women?

## Q 3. Attempt the following:

(5 x $4=20$ )
a) Prove that $[(\mathbf{p} \rightarrow \mathbf{q}) \wedge \sim \mathbf{q}] \rightarrow \sim \mathbf{p}$ is a tautology.
b) In a group of 400 people, 250 speaks English and 200 speaks konkani. Using Venn diagram find the number of people speaking both the languages.
c) Certain bank gives interest at $8.75 \%$ compounded quarterly, another bank comes up with a new scheme of simple interest at the rate of $10 \%$ per annum. Calculate which scheme is more beneficial to the customer, for the investment of 4 years.
d) If ${ }^{\mathrm{n}} \mathrm{C}_{\mathrm{r}}=120$ and ${ }^{\mathrm{n}} \mathrm{P}_{\mathrm{r}}=720$, find the value of n and r .
e) If for an A.P. fifth term is 35 and ninth term is 59 , find its $\mathrm{n}^{\text {th }}$ term.

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## OR

Q III. Attempt the following:
(5 x $4=20$ )
p) Check whether the $(\mathbf{p} \wedge \mathbf{q}) \wedge \sim(\mathbf{p} \vee \mathbf{q})$ is a contradiction or tautology .
q) Find $x$ if $\left|\begin{array}{ccc}x & 2 & 1 \\ 3 & 0 & 1 \\ 4 & 5 & -1\end{array}\right|=0$
r) Amin borrows `2000 from Sachin at compound interest of \(10 \%\) per annum, to be compounded on quarterly basis. What amount is due to him after 9 month? Also state his interest. s) 7 cards are selected from a pack of 52 cards. How many selection (i) will have exactly 3 diamonds and 4 hearts. (ii) will not contain any spade. t) A sum of` 72800 is to be paid in 6 monthly installments, such that each installment is three times the previous installment. Find the first and the last installment.

## Q 4. Attempt the following:

( $5 \times 4=20$ )
a) Vishal takes a friendly loan from his friend and promises to pay him regularly a sum of `800 at the end of each month, for a duration of 1 year. Assuming the rate of interest at \(11 \%\) compounded monthly, find the amount received by his friend at the end of the year, using the ordinary annuity principle. b) 5 students including 2 players and 3 singers seat in a line for a photograph. How many different arrangements can be done, if (i) any body can sit anywhere (ii) players can occupy end seat. c) Ajay invests` 10,000 in the first month and increases his investment by 1000 in every subsequent month. Calculate his total investment at the end of 2 years.
d) Find the principal, if the compound interest payable quarterly at $12 \%$ per annum for 2 years is ` 420 .
e) If $P=\left[\begin{array}{ll}1 & 1 \\ 2 & 0\end{array}\right]$ find the matrix $P^{2}+2 P$.

## OR

## Q IV. Attempt the following:

p) Find the present value of an ordinary annuity of ‘ 3500 p.a. for 3 years at $12 \%$ to be compounded half-yearly.

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q) From 5 professors and 7 students, a committee of 4 is to be formed. In how many ways this can be done, if the committee contains
i) Exactly 3 professors
ii) At least 3 professors.
r) For a Geometric Progression third term is 36 and sixth term is 972 , find $\mathrm{T}_{8}$.
s) Find the sum borrowed by Rahul from a bank on compound interest of $5 \%$ per year, to be calculated annually, if he had to pay back ` 26,460 after 2 years.
t) If $A=\left[\begin{array}{cc}1 & 2 \\ 2 & -1\end{array}\right]$, find the matrix $A^{2}+2 A$.

